

Please check the examination details below before entering your candidate information

Candidate surname

Other names

**Pearson Edexcel  
Level 3 GCE**

Centre Number

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Candidate Number

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**Monday 11 May 2020**

Afternoon (Time: 1 hour 40 minutes)

Paper Reference **8FM0/01**

**Further Mathematics**

**Advanced Subsidiary**

**Paper 1: Core Pure Mathematics**

**You must have:**

Mathematical Formulae and Statistical Tables (Green), calculator

Total Marks

**Candidates may use any calculator allowed by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.**

### Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided  
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

### Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 10 questions in this question paper. The total mark for this paper is 80.
- The marks for **each** question are shown in brackets  
– *use this as a guide as to how much time to spend on each question.*

### Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

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1. A system of three equations is defined by

$$\begin{aligned}kx + 3y - z &= 3 \\3x - y + z &= -k \\-16x - ky - kz &= k\end{aligned}$$

where  $k$  is a positive constant.

Given that there is no unique solution to all three equations,

- (a) show that  $k = 2$

(2)

Using  $k = 2$

- (b) determine whether the three equations are consistent, justifying your answer.

(3)

- (c) Interpret the answer to part (b) geometrically.

(1)

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2. Given that

$$z_1 = 2 + 3i$$

$$|z_1 z_2| = 39\sqrt{2}$$

$$\arg(z_1 z_2) = \frac{\pi}{4}$$

where  $z_1$  and  $z_2$  are complex numbers,

(a) write  $z_1$  in the form  $r(\cos \theta + i \sin \theta)$

Give the exact value of  $r$  and give the value of  $\theta$  in radians to 4 significant figures.

(2)

(b) Find  $z_2$  giving your answer in the form  $a + ib$  where  $a$  and  $b$  are integers.

(6)

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3.

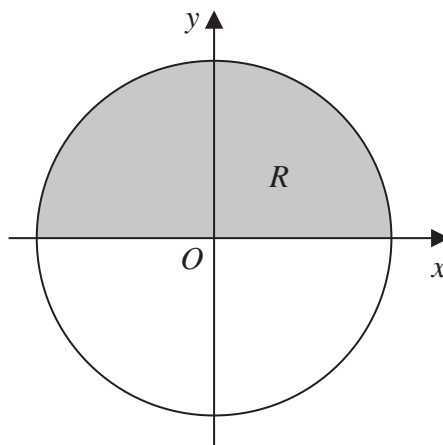


Figure 1

Figure 1 shows a circle with radius  $r$  and centre at the origin.

The region  $R$ , shown shaded in Figure 1, is bounded by the  $x$ -axis and the part of the circle for which  $y > 0$

The region  $R$  is rotated through  $360^\circ$  about the  $x$ -axis to create a sphere with volume  $V$

Use integration to show that  $V = \frac{4}{3} r^3$

(5)

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Question 3 continued

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Lined area for writing the answer to Question 3.

(Total for Question 3 is 5 marks)



4.

**All units in this question are in metres.**

A lawn is modelled as a plane that contains the points  $L(-2, -3, -1)$ ,  $M(6, -2, 0)$  and  $N(2, 0, 0)$ , relative to a fixed origin  $O$ .

(a) Determine a vector equation of the plane that models the lawn, giving your answer in the form  $\mathbf{r} = \mathbf{a} + \lambda\mathbf{b} + \mu\mathbf{c}$  (3)

(b) (i) Show that, according to the model, the lawn is perpendicular to the vector  $\begin{pmatrix} 1 \\ 2 \\ -10 \end{pmatrix}$

(ii) Hence determine a Cartesian equation of the plane that models the lawn. (4)

There are two posts set in the lawn.

There is a washing line between the two posts.

The washing line is modelled as a straight line through points at the top of each post with coordinates  $P(-10, 8, 2)$  and  $Q(6, 4, 3)$ .

(c) Determine a vector equation of the line that models the washing line. (2)

(d) State a limitation of one of the models. (1)

The point  $R(2, 5, 2.75)$  lies on the washing line.

(e) Determine, according to the model, the shortest distance from the point  $R$  to the lawn, giving your answer to the nearest cm. (2)

Given that the shortest distance from the point  $R$  to the lawn is actually 1.5 m,

(f) use your answer to part (e) to evaluate the model, explaining your reasoning. (1)

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6. (i)

$$\mathbf{A} = \begin{pmatrix} 2 & a \\ a-4 & b \end{pmatrix}$$

where  $a$  and  $b$  are non-zero constants.

Given that the matrix  $\mathbf{A}$  is self-inverse,

- (a) determine the value of  $b$  and the possible values for  $a$ . (5)

The matrix  $\mathbf{A}$  represents a linear transformation  $M$ .

Using the smaller value of  $a$  from part (a),

- (b) show that the invariant points of the linear transformation  $M$  form a line, stating the equation of this line. (3)

(ii)

$$\mathbf{P} = \begin{pmatrix} p & 2p \\ -1 & 3p \end{pmatrix}$$

where  $p$  is a positive constant.

The matrix  $\mathbf{P}$  represents a linear transformation  $U$ .

The triangle  $T$  has vertices at the points with coordinates  $(1, 2)$ ,  $(3, 2)$  and  $(2, 5)$ .

The area of the image of  $T$  under the linear transformation  $U$  is 15

- (a) Determine the value of  $p$ . (4)

The transformation  $V$  consists of a stretch scale factor 3 parallel to the  $x$ -axis with the  $y$ -axis invariant followed by a stretch scale factor  $-2$  parallel to the  $y$ -axis with the  $x$ -axis invariant. The transformation  $V$  is represented by the matrix  $\mathbf{Q}$ .

- (b) Write down the matrix  $\mathbf{Q}$ . (2)

Given that  $U$  followed by  $V$  is the transformation  $W$ , which is represented by the matrix  $\mathbf{R}$ ,

- (c) find the matrix  $\mathbf{R}$ . (2)

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7.

$$f(z) = z^4 + az^3 + bz^2 + cz + d$$

where  $a$ ,  $b$ ,  $c$  and  $d$  are real constants.

The equation  $f(z) = 0$  has complex roots  $z_1$ ,  $z_2$ ,  $z_3$  and  $z_4$

When plotted on an Argand diagram, the points representing  $z_1$ ,  $z_2$ ,  $z_3$  and  $z_4$  form the vertices of a square, with one vertex in each quadrant.

Given that  $z_1 = 2 + 3i$ , determine the values of  $a$ ,  $b$ ,  $c$  and  $d$ .

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8. Prove by induction that, for  $n \in \mathbb{Z}^+$

$$f(n) = 2^{n+2} + 3^{2n+1}$$

is divisible by 7

(6)

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10. Given that there are two distinct complex numbers  $z$  that satisfy

$$\{z: |z - 3 - 5i| = 2r\} \cap \left\{z: \arg(z - 2) = \frac{3\pi}{4}\right\}$$

determine the exact range of values for the real constant  $r$ .

(7)

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**Question 10 continued**

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Lined writing area for the answer to Question 10.



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**Question 10 continued**

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**(Total for Question 10 is 7 marks)**

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**TOTAL FOR CORE PURE MATHEMATICS IS 80 MARKS**

